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## Relation between substorm characteristics and rapid temporal variations of the ground magnetic field

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**Abstract.** Auroral substorms are one of the major causes of large geomagnetically induced currents (GIC) in technological systems. This study deals with different phases of the auroral substorm concerning their severity from the GIC viewpoint. Our database consists of 833 substorms observed by the IMAGE magnetometer network in 1997 (around sunspot minimum) and 1999 (rising phase of the sunspot cycle), divided into two classes according to the  $D_{st}$  index: non-storm ( $D_{st} > -40$  nT, 696 events) and storm-time ones ( $D_{st} < -40$  nT, 137 events). The key quantity concerning GIC is the time derivative of the horizontal magnetic field vector ( $d\mathbf{H}/dt$ ) whose largest values during substorms occur most probably at about 5 min after the onset at stations with CGM latitude less than 72 deg. When looking at the median time of the occurrence of the maximum  $d\mathbf{H}/dt$  after the expansion onset, it increases as a function of latitude from about 15 min at CGM lat=56 deg to about 45 min at CGM lat=75 deg for non-storm substorms. For storm-time events, these times are about 5 min longer. Based on calculated ionospheric equivalent currents, large  $d\mathbf{H}/dt$  occur mostly during the substorm onset when the amplitude of the westward electrojet increases rapidly.

**Keywords.** Geomagnetism and paleomagnetism (Rapid time variations) – Ionosphere (Auroral ionosphere) – Magnetospheric physics (Storms and substorms)

### 1 Introduction

Associated with geomagnetic variations, geomagnetically induced currents (GIC) flow in technological conductor systems such as power grids and pipelines (e.g. Boteler et al., 1998; Kappenman, 1996, 2005; Molinski, 2002). The basic principle follows from Faraday's law linking temporal

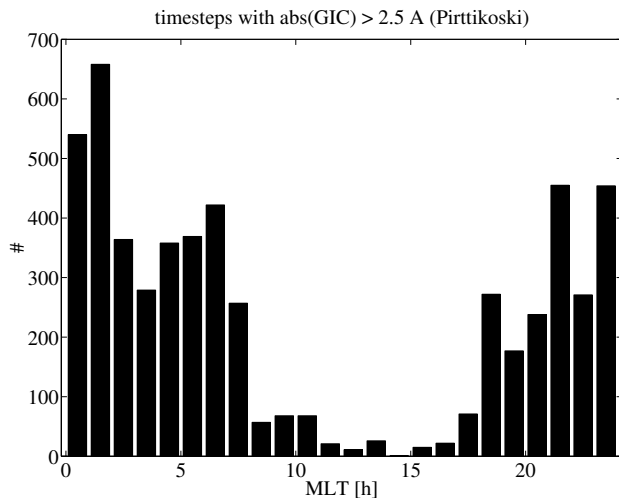
changes of the magnetic flux to the electromotive force. So a geoelectric field is always associated with a temporally varying geomagnetic field. This means that the time derivative of the ground magnetic field ( $d\mathbf{B}/dt$ ) characterizes GIC activity. More explicitly, the horizontal component of the vector ( $d\mathbf{H}/dt$ ) is the relevant quantity (Viljanen et al., 2001). Calculation of GIC is practical in two independent steps: 1) determine the (horizontal) electric field at the earth's surface, 2) determine induced currents driven by this electric field in a specified conductor system. One technique used in postanalysis of GIC events is presented by Viljanen et al. (2004).

The ability to derive GIC statistics based on magnetic recordings can help utilities to estimate which parts of a conductor system might be susceptible to GIC effects. However, this does not help in preventing immediate damages, which may develop in a few minutes during magnetic disturbances. The best-known cases concerning power system failures are the Québec blackout in Canada in March 1989 (Bolduc, 2002), and the Malmö blackout in Sweden in October 2003 (Pulkkinen et al., 2005; Rosenqvist et al., 2005).

The present solar wind observations at the L1 point allow for a 30–60 min warning time in practice. It would be ideal if GIC forecasts could be provided at least one hour prior to anticipated large events, because certain system operating changes can take 1–2 h to complete (Molinski, 2002).

Exact local warnings would require that  $d\mathbf{B}/dt$  could be forecasted as a time series close to the sites where GIC are of interest. The surface grid could be quite sparse (of a 100-km scale), but it would be critical to predict  $d\mathbf{B}/dt$  accurately, especially concerning the largest values. Weigel et al. (2003) has attempted to forecast the 30-min average absolute magnitude of  $d\mathbf{B}/dt$  directly from solar wind observations. The highest prediction efficiencies achieved are about 0.7. The success of the prediction is highly dependent on the spatial location and on the local time. Wintoft (2005) showed that the 10-min log-root-mean-square of  $dX/dt$  and  $dY/dt$

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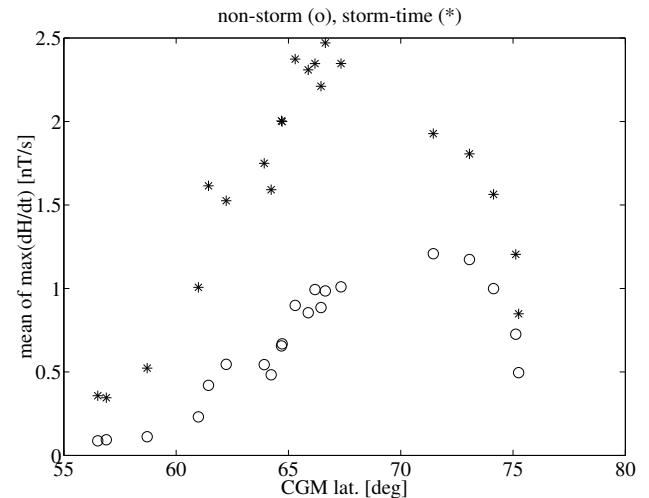


**Fig. 1.** Diurnal variation of the number of observations in 1999–2000 when the absolute value of GIC (10-s data) exceeded 2.5 A at the Pirttikoski 400-kV transformer in northern Finland. The corrected geomagnetic (CGM) latitude of this site is about 63 deg N. The figure is taken from Viljanen et al. (2001).

at two subauroral locations may be predicted up to 30 min in advance with a linear correlation coefficient close to 0.8.

The main difficulty in GIC forecasting is obviously the large variability of the length scales of ionospheric current systems relevant to GIC (Pulkkinen et al., 2003a,b). Viljanen et al. (1999) listed some event types in their Table 1, during which large GIC may occur. A manual rough classification of one-year GIC data indicated that rapid enhancements of large-scale auroral electrojets, substorm onsets, pulsations, and sudden impulses have caused significant GIC. The diurnal occurrence of large GIC values at one site in northern Finland is shown in Fig. 1. There is a clear maximum around the magnetic midnight corresponding most probably to substorm activity. This gives the motivation for this paper to investigate auroral substorms in detail from the GIC viewpoint. Since GIC measurements are not available as extensively as magnetic recordings, we use the latter ones.

An enhanced geomagnetic activity is obviously a precondition for the occurrence of large GIC. However, a large magnetic variation field  $\mathbf{B}$  itself does not necessarily imply that  $d\mathbf{B}/dt$  is also large, and vice versa. As shown by Viljanen et al. (2001), large  $d\mathbf{B}/dt$  events are nearly always related to westward ionospheric currents. However, the directional distributions of the horizontal time derivative vector ( $d\mathbf{H}/dt$ ) are much more scattered than those of the simultaneous horizontal variation field vector ( $\mathbf{H}$ ). This is possible only if there are rapidly changing ionospheric current systems of a length scale of 100 km or less embedded in a smooth background east-west flow. Pulkkinen et al. (2003a), Pulkkinen et al. (2003b) and Viljanen et al. (2004) have demonstrated this



**Fig. 2.** Average of  $\max(|d\mathbf{H}/dt|)$  during substorms as a function of the CGM latitude. Circles: non-storm substorms, asterisks: storm-time substorms.

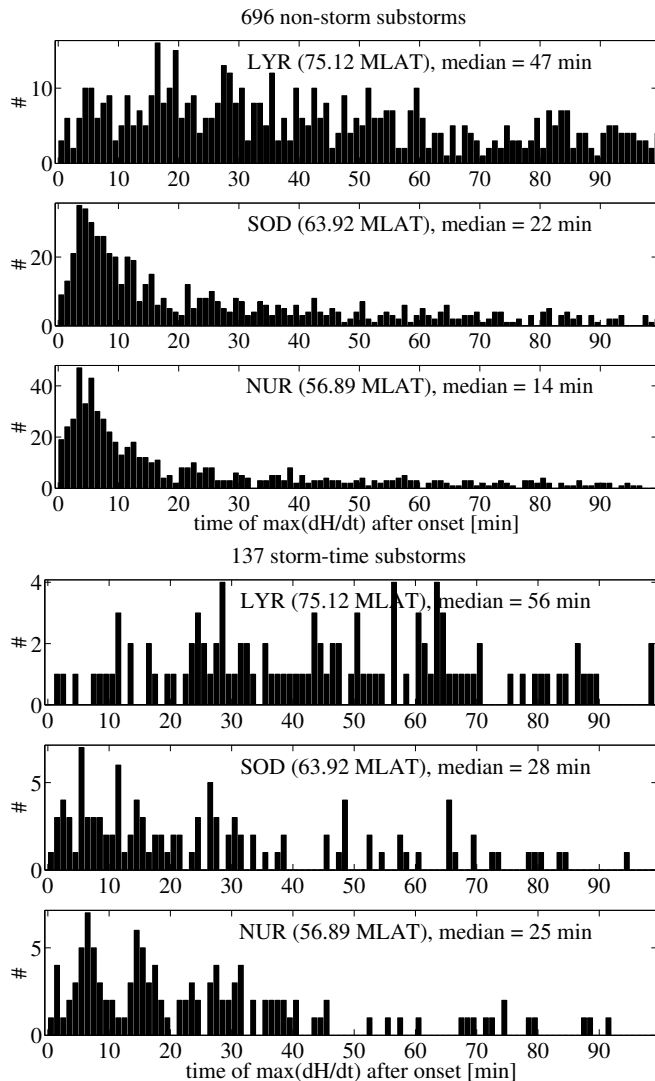
with single events. It is obvious that GIC forecasting cannot be based on solar wind data only, but conditions in the magnetosphere and ionosphere are important too.

The main science question to which we are looking for an answer in this paper is how the GIC activity varies during different substorm phases. We start examining characteristics of  $d\mathbf{H}/dt$  followed by a study of the temporal and spatial behaviour of ionospheric equivalent currents during substorms.

## 2 Results

### 2.1 Data description

Our database consists of 833 substorms in 1997 (around sunspot minimum) and 1999 (rising phase of the sunspot cycle 23) observed by the IMAGE magnetometer network in northern Europe (Tanskanen et al., 2002). IMAGE covers the magnetic latitudes where the electrojets related to substorms are flowing. We used the local variant of the AL index (IL index) to define a substorm. We looked for negative bay-type variations of IL ( $>100$  nT) showing a clear onset when IL rapidly decreases at least 100 nT within 10 min. We considered the periods between 16:00 UT and 02:00 UT (about 18:00–04:00 MLT), when IL gives a good estimate of the global AL. The exact timing of the onset is somewhat subjective, so there is a couple of minutes inaccuracy. We divided the events into two classes, non-storm and storm-time ones, according to the  $D_{st}$  index. The value of  $D_{st}$  is smaller than  $-40$  nT for storm-time substorms and larger than  $-40$  nT for non-storm ones, respectively (Kallio et al., 2000). In this dataset, there are 696 non-storm and 137 storm-time substorms (from the original list of Tanskanen et al. (2002),



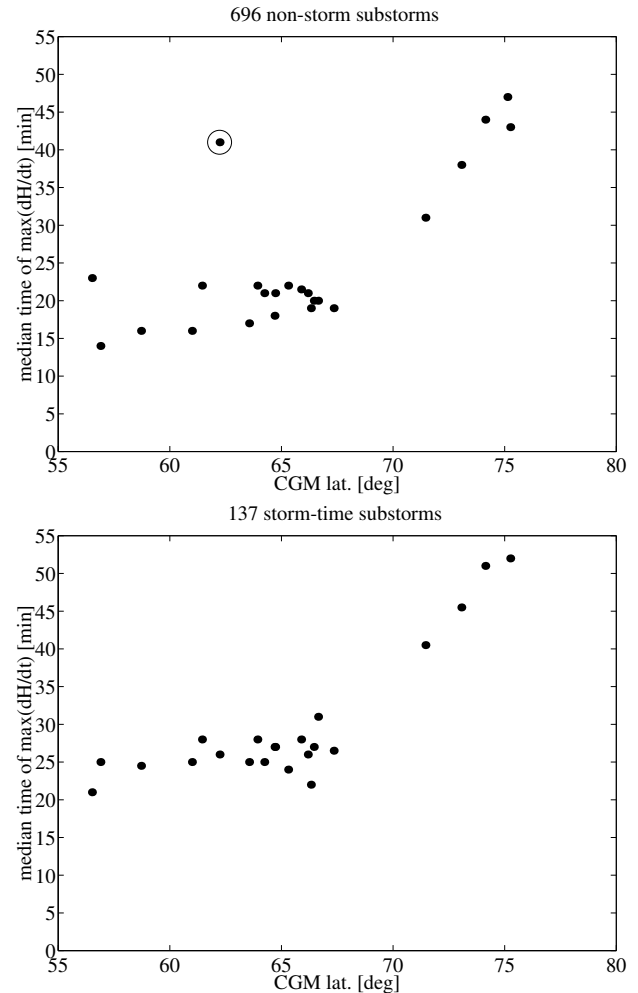
**Fig. 3.** Time of  $\max(|d\mathbf{H}/dt|)$  after the substorm onset at three IMAGE sites: LYR, SOD, NUR. Upper panel: non-storm substorms, lower panel: storm-time substorms.

6 events were omitted). The time resolution of the magnetic data is 1 min.

We use the magnetic variation field from which the quiet-time baseline is subtracted. The baselines have been selected visually for each day separately. The time derivative of the field is the difference between two successive values divided by the sampling interval, and it is independent of the baseline. One minute is still a sufficiently short time step to reveal characteristic features of  $d\mathbf{H}/dt$ .

## 2.2 Characteristics of $d\mathbf{H}/dt$

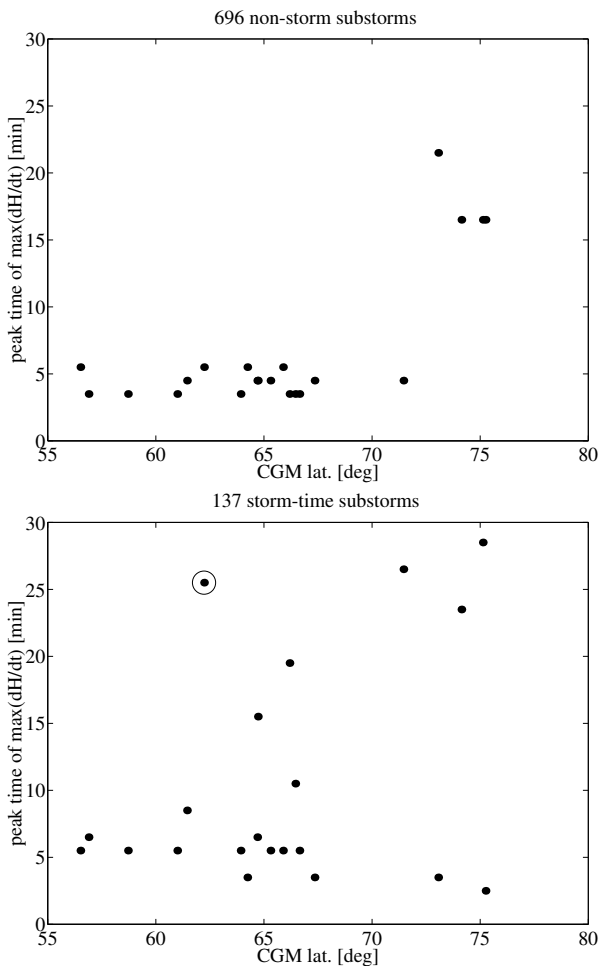
The average of the maximum  $|d\mathbf{H}/dt|$  at each IMAGE site is shown in Fig. 2. During storm-time substorms,



**Fig. 4.** The median time of  $\max(|d\mathbf{H}/dt|)$  after the onset as a function of the CGM latitude. Upper panel: non-storm substorms, lower panel: storm-time substorms. A clear outlier is marked by a circle.

$\max(|d\mathbf{H}/dt|)$  is approximately twice the value of non-storm substorms at all latitudes. The site of maximum  $|d\mathbf{H}/dt|$  as a function of latitude is about 5 deg more southward for storm-time than for non-storm substorms. The gap between the latitudes 67 and 71 is due to the Arctic Ocean between the mainland and Bear Island.

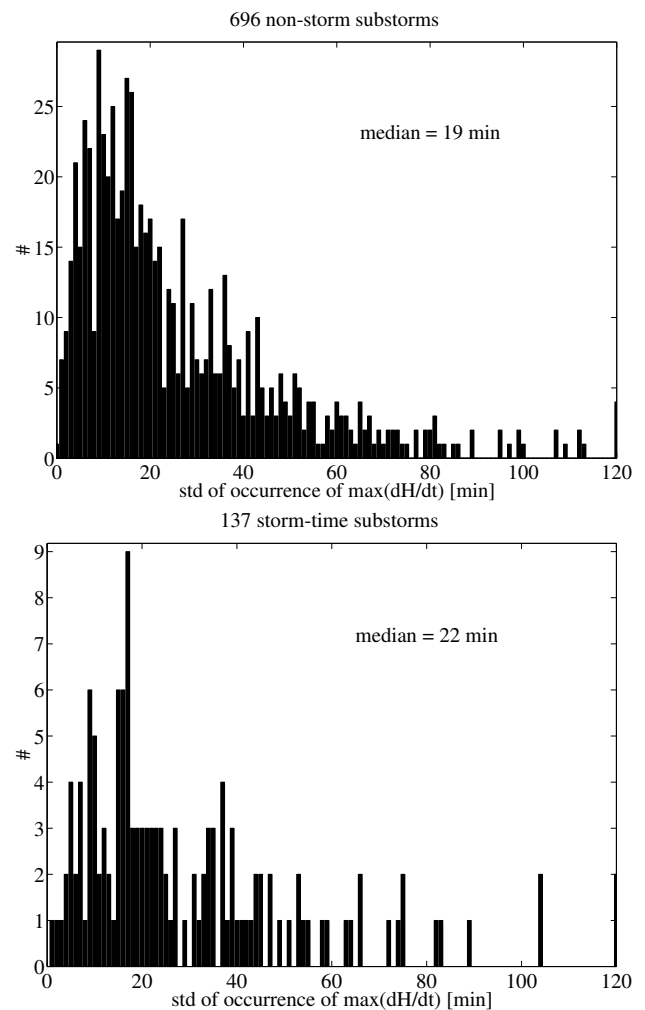
The occurrence time of  $\max(|d\mathbf{H}/dt|)$  after the substorm onset at each available magnetometer site gives an overview of the GIC activity during substorms. Examples of occurrence distributions at single sites are shown in Fig. 3. For non-storm substorms, distributions are sharply peaked at lower latitudes (NUR, SOD) as indicated by the maxima at about 5 min after the onset. However, there is still a clear tail in the distribution, which is typical for complex multiscale systems (Sornette, 2004). Distributions of  $\max(|d\mathbf{H}/dt|)$  are scattered for storm-time substorms at all sites, which may



**Fig. 5.** The most probable time of  $\max(|d\mathbf{H}/dt|)$  after the onset as a function of the CGM latitude. Upper panel: non-storm substorms, lower panel: storm-time substorms. A clear outlier is marked by a circle.

also be due to the relatively small number of data. For a more quantitative comparison of the distributions, we performed a simple  $\chi^2$  test (e.g. Press et al., 2002) between pairs of stations using time bins from 0 to 60 min. We then obtained the following  $\chi^2$  values with the corresponding probabilities in parantheses. Non-storm substorms yield NUR-SOD 47.3 (0.86), NUR-LYR 244 (0.00), SOD-LYR 187 (0.00), and storm-time cases yield NUR-SOD 36.2 (0.99), NUR-LYR 70.1 (0.15), SOD-LYR 74.9 (0.08). This means roughly that the distributions at LYR are really different from those at SOD and NUR, whereas SOD and NUR are quite similar to each other.

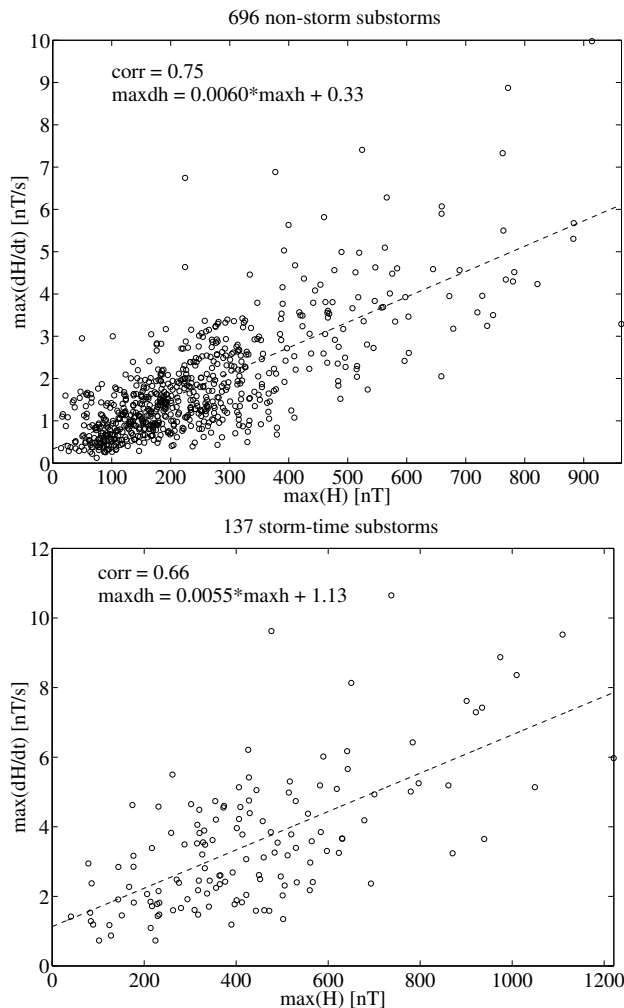
The median value of the occurrence time of  $\max(|d\mathbf{H}/dt|)$  increases as a function of latitude (Fig. 4) for both non-storm and storm-time cases. The Svalbard stations (CGM lat  $> 70$ ), including Bear Island, differ clearly from the continental sites. In the non-storm case the station at CGM lat 62.23



**Fig. 6.** Simultaneity of the occurrence of  $\max(|d\mathbf{H}/dt|)$  after the onset at the IMAGE sites. The histogram presents the standard deviation of the maxima times. Events with data from at least 15 stations are taken into account. Upper panel: non-storm substorms, lower panel: storm-time substorms.

(Rørvik) is a clear outlier due to the small amount of available data.

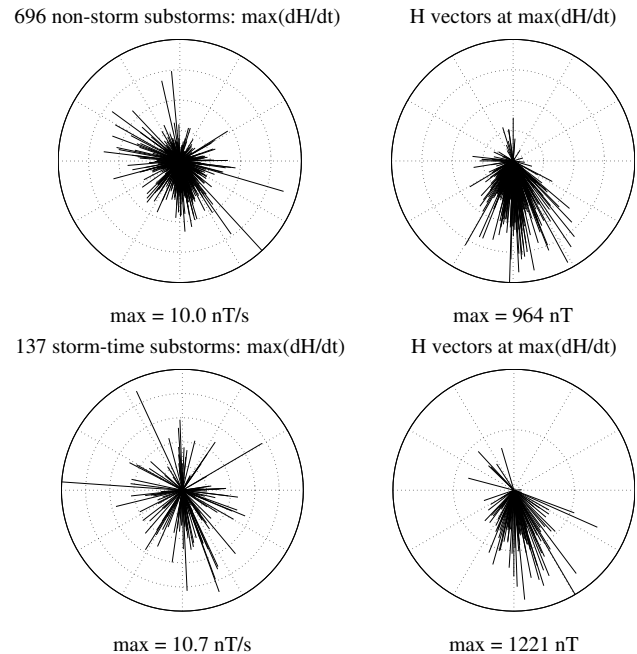
When the most probable occurrence time of  $\max(|d\mathbf{H}/dt|)$  after onset is considered (Fig. 5), the situation becomes more complex. For non-storm substorms, the four sites in Svalbard (CGM lat  $> 73$ ) and the continental sites and Bear Island (CGM lat  $< 71.5$  deg) still comprise two distinct sets. The Svalbard stations are mostly north of the auroral oval around the local midnight (cf. Kauristie, 1995), so they do not show typical substorm features. Storm-time events in turn have quite an irregular behaviour as a function of latitude, evidently due to the small number of datapoints. However, also for them, the most probable maximum time is about 5 min after the onset at lowest latitudes.



**Fig. 7.** The  $\max(|d\mathbf{H}/dt|)$  versus  $|\mathbf{H}|$  at the maximum times of  $|d\mathbf{H}/dt|$  during non-storm (upper panel) and storm-time (lower panel) substorms. The dashed line is the linear regression curve.

The characteristics of a GIC event also depend on how simultaneously large  $d\mathbf{H}/dt$  values occur. To quantify this, we have collected maximum times of  $d\mathbf{H}/dt$  at all sites and calculated the standard deviation of them for each event. To have a good spatial coverage, we have only considered events with data available at least from 15 sites. A complete simultaneity would produce a zero standard deviation, but in practice there is much scattering with a clearly tailed distribution as shown in Fig. 6. The simultaneity does not directly give any information about GIC values at a specific site, since the geometry of the induced geoelectric field should also be known.

An interesting open question is how closely  $|d\mathbf{H}/dt|$  is related to  $|\mathbf{H}|$ . Knowing the relationship may improve forecasting possibilities. There is already quite a good success in predicting  $|\mathbf{H}|$  or indices based on it, like AE (Gleisner

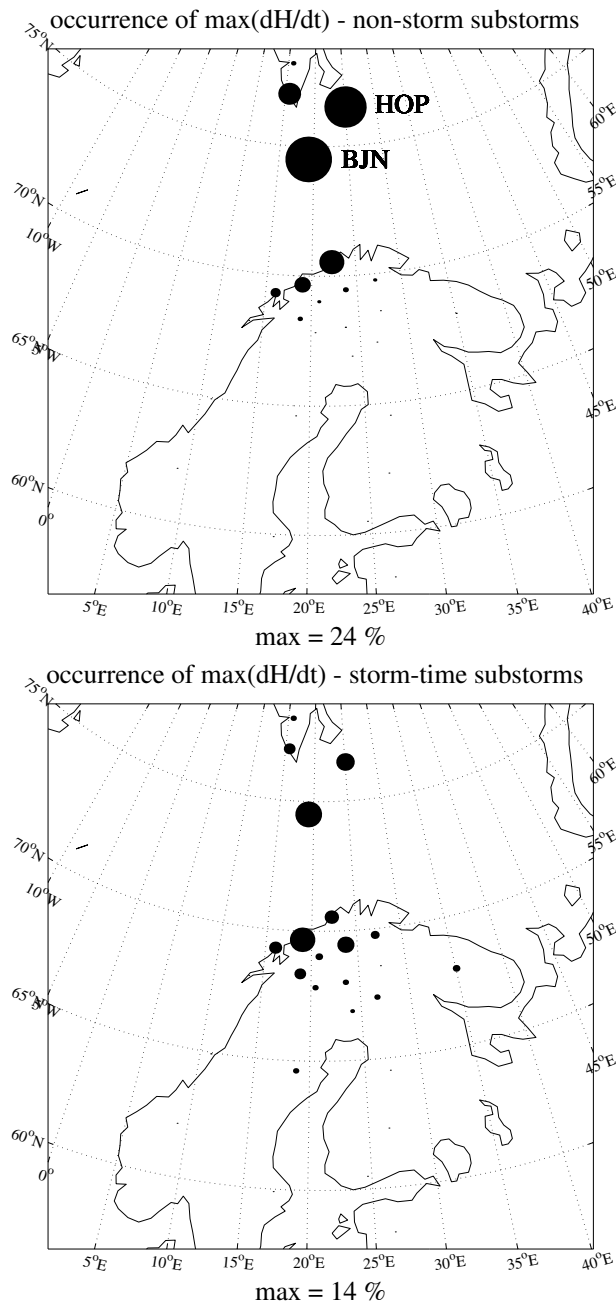


**Fig. 8.** Upper row:  $\max(d\mathbf{H}/dt)$  vectors of non-storm substorms, and simultaneous  $\mathbf{H}$  vectors at the maximum sites of  $d\mathbf{H}/dt$ . Lower row: the same for storm-time substorms. The north direction is up and the east direction to the right.

and Lundstedt, 1997). The relation between  $\max(|\mathbf{H}|)$  and  $\max(|d\mathbf{H}/dt|)$  for non-storm and storm-time substorms are shown in Fig. 7. These plots deal with the maximum value of  $|d\mathbf{H}/dt|$  during each substorm with the simultaneous  $|\mathbf{H}|$  at the maximum site of  $|d\mathbf{H}/dt|$ . There is quite a high correlation between  $|\mathbf{H}|$  and  $|d\mathbf{H}/dt|$ , 0.75 for non-storm and 0.66 for storm-time substorms. However, for a given  $|\mathbf{H}|$ , the range of  $|d\mathbf{H}/dt|$  values is roughly  $\pm 2$  nT/s. The slope of the regression curve is nearly the same for both types of substorms. This indicates that the (substorm) mechanism behind the relation between  $\mathbf{H}$  and  $d\mathbf{H}/dt$  may be independent of storm conditions.

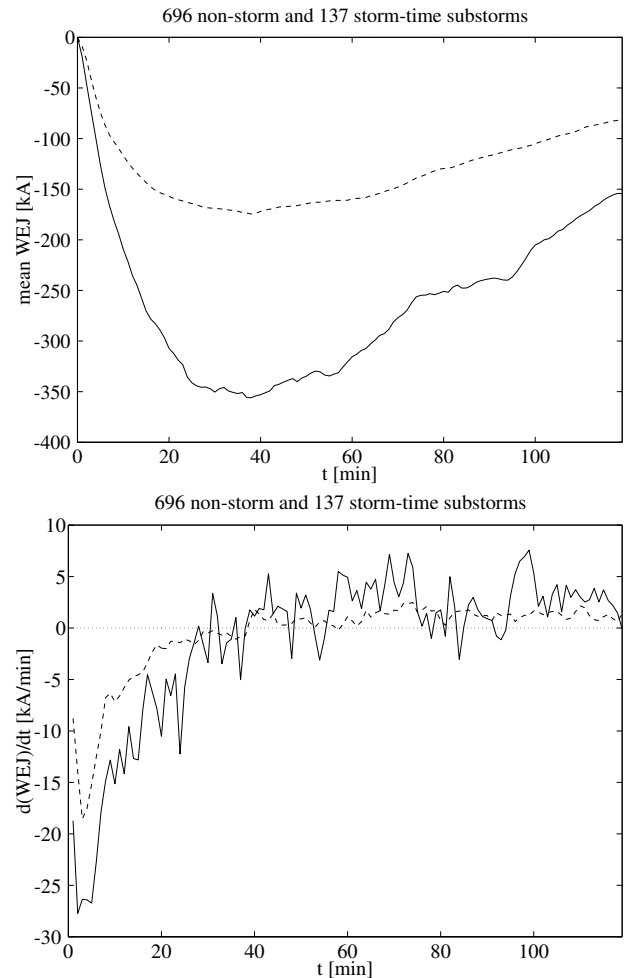
A clear majority of  $\max(|d\mathbf{H}/dt|)$  is associated with a westward electrojet as shown in Fig. 8, since a southward variation field is due to a westward (equivalent) current flow in the ionosphere. The scattering of  $d\mathbf{H}/dt$  means that rapid changes are not always due to an increase or decrease of the electrojet current, but they are often related to some smaller scale structures like vortices (Viljanen et al., 2001; Apatenkov et al., 2004).

The spatial occurrence of the maximum  $d\mathbf{H}/dt$  is shown in Fig. 9. The average maximum site is more southward for storm-time substorms, and reflects the well-known shift of the auroral oval equatorwards during increased magnetic activity (e.g. Rostoker and Phan, 1986; Ahn et al., 2005). The same feature is obvious in Fig. 2. The dominance of some



**Fig. 9.** Spatial occurrence distribution of the maximum site of  $d\mathbf{H}/dt$  during non-storm (upper panel) substorms and storm-time substorms (lower panel).

sites is partly due to the local conductivity of the earth's uppermost crust: the larger the conductivity the larger  $d\mathbf{H}/dt$  can be at short periods with small skin depths (Viljanen et al., 2001). Especially, the high conductivity of the ocean water has an obvious effect at BJN and HOP stations. On the other hand,  $\mathbf{H}$  is less sensitive to the local earth conditions, since its power spectrum has largest amplitudes at longer periods

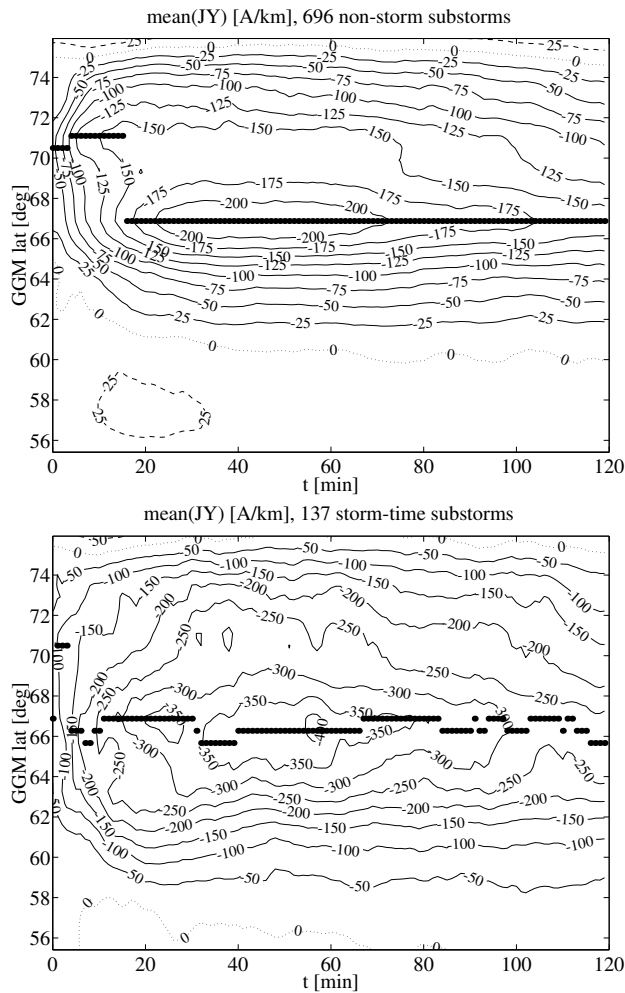


**Fig. 10.** Mean total westward electrojet (WEJ) and its time derivative during a non-storm (dashed line) and a storm-time substorm (uniform line). The origin of the time axis is the substorm onset, when the current is set to zero.

than the time derivative. Consequently, relevant skin depths are larger for  $\mathbf{H}$  than for  $d\mathbf{H}/dt$ .

### 2.3 Ionospheric equivalent currents

Ionospheric equivalent currents have been calculated using the method of spherical elementary current systems (Amm, 1997; Pulkkinen et al., 2003a). The current density was determined along the geographic longitude 22.06 deg E from the latitude 59.02 N to 79.42 N with a 0.6-deg spacing. Since we did not separate the ground magnetic field into external and internal parts, the equivalent current actually contains the induced currents in the earth. This overestimates the ionospheric contribution up to 40% at onset times close to the maximum current flow (Tanskanen et al., 2001). However, it is not a drawback from the viewpoint of the present study,

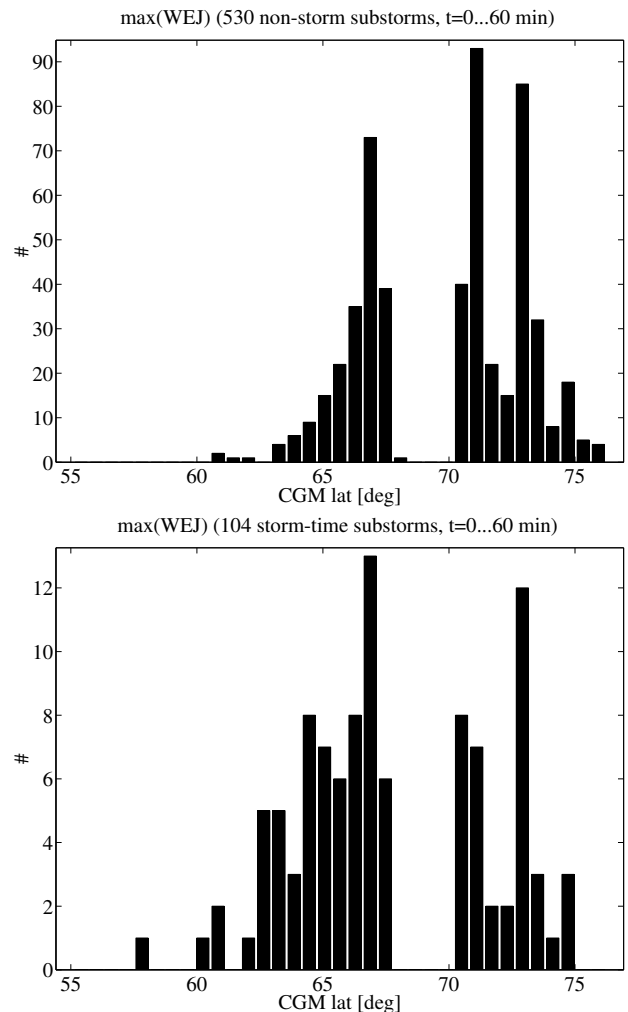


**Fig. 11.** Average eastward equivalent current density ( $JY$ ) during 120 min after the onset at  $t=0$ . Negative values marked by negative contour lines mean a westward current. Dots show the location of the maximum westward current density. Upper panel: non-storm substorms, lower panel: storm-time substorms.

since GIC is related to the total  $d\mathbf{H}/dt$  at the earth's surface.

The mean temporal behaviour of the total westward current is shown in Fig. 10. We set the total current to zero at the onset time, which does not affect the shape of the curves. The curves shown in the figures are the averages of all events. The time derivative was calculated from the average curve of the total current. As expected, the total current is more intense during storm-time events. The maximum of the derivative occurs a few minutes after the onset, which is consistent with Fig. 3 (stations NUR and SOD). Due to using the integrated total electrojet, the behaviour of the time derivative reflects mostly the large-scale characteristics of ionospheric currents.

The average equivalent ionospheric current density with respect to time and magnetic latitude is shown in Fig. 11.



**Fig. 12.** Distribution of the latitude of the maximum of the westward equivalent current (WEJ) density at the moment of the maximum  $d\mathbf{H}/dt$ . Only timesteps within 60 min after the onset are taken into account.

The largest westward current takes place at about geomagnetic latitude 70.5, 1 deg south of Bear Island (BJN in Fig. 9). However, during storm-time substorms, the maximum moves in a few minutes 4 deg southward above the continental coastline. The same happens for non-storm cases, but only after about 15 min after the onset. When analysing these features, we must note that there is a gap in IMAGE between latitudes 67.5 and 70.5 due to the Arctic Ocean. Furthermore, the network is sparse north of Bear Island too. The method to calculate equivalent currents does not tend to produce maxima of the current density in such gaps. It follows that the prominent asymmetry in the latitudinal distribution of the current density may not be true.

The latitude of the maximum westward current density at the moment of the maximum  $d\mathbf{H}/dt$  is shown in Fig. 12. It



is very rare that the maximum takes place at CGM latitudes lower than 60. This is in a good agreement with the results by Ahn et al. (2005). Again, the gap between latitudes 67.5 and 70.5 is an artifact due to the lack of stations. Finally, we determined the latitude of the maximum westward current density at the time of the largest  $|d\mathbf{H}/dt|$  after onset. It is quite well linearly related to the latitude of  $\max(|d\mathbf{H}/dt|)$  with the correlation coefficient of 0.78.

### 3 Conclusions

The key quantity concerning geomagnetically induced currents is the time derivative of the horizontal magnetic field vector ( $d\mathbf{H}/dt$ ), which is available on wide ground networks with good spatial and temporal coverages. Based on the study of 833 substorms, the largest values of  $d\mathbf{H}/dt$  occur most probably during the substorm expansion phase at about five min after the expansion onset at stations with CGM latitudes less than 72 deg. However, the occurrence distribution has a long tail extending to tens of minutes. When looking at the median time of the occurrence of the maximum  $d\mathbf{H}/dt$  after the onset, it increases as a function of latitude from about 15 min at CGM lat 56 deg to about 45 min at CGM lat 75 deg for non-storm substorms.

The maximum  $d\mathbf{H}/dt$  can have a large east-west component compared to the north-south one, whereas the simultaneous  $\mathbf{H}$  is more concentrated into the southward direction. This indicates that in addition to the rapid change of the main electrojet, there are often ionospheric structures of smaller scales having a comparable effect on  $d\mathbf{H}/dt$ . In this sense, there seems to be no differences between non-storm and storm-time substorms except for in amplitudes, which are larger for the latter ones, and occur more southward. McPherron and Hsu (2002) found no qualitative distinction between the various classes of substorms, but they are likely to be caused by the same mechanism, and our results give some further support to this.

In this paper the relationship between the GIC activity, characterised by the time derivative of the ground magnetic field, and substorm activity was examined for two years of which 1997 occurs around the sunspot minimum and 1999 at the rising phase of the sunspot cycle 23. A future study is needed to explore the GIC-substorm relationship in the descending sunspot cycle phase, when high speed streams are known to have a large effect on the substorm activity (Tanskanen et al., 2005).

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